## Mathematics Properties

| $\mathrm{a}=\mathrm{a}$ | If something is equal to its identical twin | Reflexive Property |
| :---: | :---: | :---: |
| $\mathrm{a}=\mathrm{b} \& \mathrm{~b}=\mathrm{a}$ | If something flipped sides of the equal sign | Symmetric Property |
| $\mathrm{a}=\mathrm{b}, \mathrm{c}=\mathrm{b}$ so $\mathrm{a}=\mathrm{c}$ | If two items are equal to a third item, the two are equal | Transitive Property |
| $a+b=b+a$ | If you reversed the order of addition or multiplication | Commutative Property |
| $a+(b+c)=(a+b)+c$ | If you changed a grouping rearranged parenthesis, but kept everything else in the same order | Associative Property |
| If $a=b$ then $a+c=b+c$ | If you added the same non-zero \# to both sides | Addition Property |
| If $\mathrm{a}=\mathrm{b} \mathrm{ac}=\mathrm{bc}$ | If you multiplied the same nonzero \# to both sides you have used the | Multiplication Property |
| $a+0=a$ | If you added 0 to get the same \# back | Additive Identity |
| (a) $1=a$ | If you multiplied by 1 to get the same \# back | Multiplicative Identity |
| $a+(-a)=0$ | If you added opposite \#'s and ended with 0 | Property of Opposites |
| (b) $1 / b=1$ | If you multiplied by a reciprocal to get 1 | Property of Reciprocals |
| $\begin{aligned} & a(b+c)=a b+a c \\ & q r+r s=(q+s) r \end{aligned}$ | If you multiplied a \# into or pulled a \# out of parenthesis | Distributive Property |
| (a) $0=0$ | If you multiplied by 0 and got 0 | Multiplication Property of 0 |
| $W(-1)=-w$ | If you multiplied by ( -1 ) and got the opposite of what you started with | Multiplicative Property of (-1) |
|  | If you have stated that $\mathrm{a}<\mathrm{b}, \mathrm{a}=\mathrm{b}$ or $\mathrm{a}>\mathrm{b}$ | Comparison Property |
| $\begin{aligned} & a<b, c \text { is }+ \text {, then } \\ & a c<b c \end{aligned}$ | If you multiplied an inequality by a positive \# and maintained the inequality | $1^{\text {st }}$ Multiplication Property of Order |
| $\begin{aligned} & a<b, c \text { is }- \text {, then } a c \\ & >b c \end{aligned}$ | If you multiplied as inequality by a negative \# and reversed the inequality | $2^{\text {nd }}$ Multiplication Property of Order |
| $\begin{aligned} & a+c=b+c \text { then } \\ & a=b \end{aligned}$ | If you cancelled the same quantity from both sides of an equation (by subtracting) | Cancellation Property of Addition |
| $\mathrm{ac}=\mathrm{bc}$ so $\mathrm{a}=\mathrm{b}$ | If you cancelled the same nonzero quantity from both sides of an equation (by division) | Cancellation Property of Multiplication |
| $\begin{aligned} & a b=0 \text { if } a=0 \text { or } \\ & b=0 \end{aligned}$ | If a product is zero, so you know that one of the factors has to be zero | Zero Product Property |
| $\mathrm{a} / \mathrm{b}=(\mathrm{a})^{1} / \mathrm{b}$ | If you changed a division to multiplication by a reciprocal | Definition of Division |
| $a+(-b)=a-b$ | If you have switched from adding a negative to just subtraction, or vice versa | Definition of Subtraction |
| $(x) x=x^{2}$ | If you have either broken apart exponents or created an exponent by multiplying a number by itself | Definition of Exponents |
|  | If you have replaced one statement with an equivalent one and no other property or definition works | Substitution Property |

